Da Coda Al Fine
Pushing Octave’s Limits

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Octave is the Matlab®-clone which comes closest to the original. Though it tries to be fully compatible, it features its own extensions and improvements over the functionality of the commercial Matlab® product.

Octave is shipped with a 340+ page reference manual, which also tries to be a bit of a user guide. Despite its size the documentation is incomplete, and where it stops, Coda starts: Da Coda Al Fine approaches Octave purely from the user’s point of view, explaining e.g. `.oct`-file construction in a tutorial like form.

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Chapter 1. oct Files

Octahedron, octopus, oculist, oct-file? – What?

An oct-file is a dynamical extension of the Octave interpreter, in other words a shared library or shared object. The source files, that make up an oct-file, are written in C++, and therefore, conventionally, carry the extension cc.

Why would you ever want to write in C++ again, having the wonderful Octave environment at your service? Well, sometimes the performance of native Octave-code is not enough to attack a problem. Octave-code is interpreted, thus it is inherently slow when executed (especially if the problem cannot be vectorised). In such a case moving from m-code to compiled C++-code speeds up the execution by a factor of ten or more. The second group of problems, where reverting to low-level code is necessary, is when interfacing with foreign libraries (think of LAPACK) or routines written in languages other than C++, most notably Fortran-77.

Having convinced ourselves that we have to bite the bullet, we start with an easy tutorial (Section 1.1). This will teach any reader who is sufficiently used to C++ how to write her first dynamically linked extension for Octave. Having guided the reader with her first steps, Section 1.2 covers more advanced topics of writing extensions. For later reference, we provide a quick reference of the most helpful methods of the Octave interface classes in Section 1.3.

1.1. Tutorial

The tutorial unfurls slowly; we do not want to scare anybody by the complexity of the task ahead. At any time, if you feel like it, look into the directories OCT/src or OCT/src/DLD-FUNCTIONS, where OCT is the root directory of your Octave source-tree and consult the header-files and already existent dynamic extensions.

1.1.1. Problem Definition

Instead of giving an abstract treatise, we want to explain the whole business of dynamical extensions with the help of a simple, yet non-trivial problem. This example shall be analyzed in detail from beginning to end, and we shall elucidate some modern software construction principles on the way.

We shall implement a matrix power function.\(^1\) Given a square matrix \(A\) of integers, reals, or complex values, and a non-negative integral exponent \(n\), the function \texttt{matpow}(\(A\), \(n\)) is to calculate \(A^n\).

We have to watch out for boundary cases: an empty matrix \(A\) or a zero exponent \(n\).
1.1.2. High-Level Implementation

We postpone writing the C++-implementation until we are completely satisfied with our implementation in Octave. Having Octave, a rapid prototyping environment at hand, it would be stupid to throw away its possibilities.

Hobby Astronomer’s Mirror Making Rule

It is faster to grind a 3 inch mirror and then a 5 inch mirror, that to grind a 5 inch mirror.

Now that the problem is exactly defined, we can start thinking about an implementation. Here is our naive first shot:

Example 1-1. Naive implementation of matpow

```matlab
function b = matpow0(a, n)
    ## Return b = a^n for square matrix a, and non-negative, integral n.
    ## Note: matpow0() is an extremely naive implementation.
    b = diag(ones(size(a, 1), 1));
    for i = 1:n
        b = b * a;
    endfor
endfunction
```

Easy does the job! matpow0 looks like it does what we want, but how can we be sure? We write a test-suite2! A test-suite is needed when we switch to C++. We have a piece of running code, so let us write some tests. The unit testing functions are defined in Appendix A, Section A.1.

```matlab
### name: test_matpow.m -- test matrix power functions
### original: Ch. L. Spiel
###
### The following tests should succeed.
###
### unit_init(0, {"a"}); ## Quiet testing, use global variable a

a = [ 2.0, -3.0; -1.0, 1.0];

unit_test_equals("a^0", matpow0(a, 0), diag([1, 1]));
unit_test_equals("a^1", matpow0(a, 1), a);
unit_test_equals("a^2", matpow0(a, 2), a^2);
unit_test_equals("a^3", matpow0(a, 3), a^3);
unit_test_equals("a^4", matpow0(a, 4), a^4);
unit_test_equals("a^22", matpow0(a, 22), a^22);
unit_test_equals("a^23", matpow0(a, 23), a^23);
```
Running the tests on matpow0 gives us confidence

octave:2> test_matpow

..............
# of testcases attempted 7
# of expected passes 7
# of expected failures 0
# of unexpected passes 0
# of unexpected failures 0
# of unresolved testcases 0

but we also get more ambitious!

Our algorithm is really naive, and matrix multiplications are computationally expensive. Let us cut down on the number of multiplications. What is the minimum number of multiplications needed to compute $A^n$? Starting with $A$, we can only square it, getting $A^2$. Again squaring is the fastest way to get to the fourth power. In general squaring our highest power lets us advance with least multiplications. This is the heart of our new algorithm.

**Improved matrix power algorithm.** If the exponent $n$ is a $w$-bit number, we can apply the binary expansion $n = \sum (b_i \times 2^i, i = 0..w-1)$, where the $b_i$ are either 0 or 1. In other words, we square $A$ for every bit in the binary expansion of $n$, multiplying this value with the final result if $b_i = 1$. Special care has to be taken for the cases where $n = 0$ or 1. See also [Golub:1996], section 11.2.5, page 569.

**Example 1-2. Implementation of improved matrix power algorithm**

```matlab
function b = matpow1(a, n)
    ## Return b = a^n for square matrix a, and non-negative, integral n.

    -- handle special cases: n = 0, and n = 1
    -- first, to allow for an early return
    if (n == 0)
        b = diag(ones(size(a, 1), 1));
        return;
    endif

    if (n == 1)
        b = a;
        return;
    endif

    -- general case: n >= 2
    p = a;                            -- p holds the current square
    b = a;
```

---

### print results

```matlab
unit_results();
```

---
The new algorithm reduces the number of matrix multiplications from $O(n)$, to $O(\log_2(n))$, which is a remarkable improvement for large matrices as matrix multiplication itself is an $O(m^3)$ process ($m$ is the number of rows and columns of the matrix).

Running the test-suite again ensures that we did not code any nonsense.

### 1.1.3. Our First Dynamic Extension

Ready for the jump to light speed? Wait – we have to feed the navigation computer first!

#### 1.1.3.1. Feature Compatibility

In principle, the functions defined in `oct`-files must have the same capabilities as functions in `m`-files. In particular, the input and output arguments lists must be able to carry different numbers of arguments, which are moreover of different type, just as `m`-file functions can. This means that there must be a way of mapping a function from Octave like

```octave
function [array, real-scalar, integer] =
  func(complex-scalar, array, list, integer)
  ## func frobs the snafu, returning all gromniz coefficients.
  -- actual function code goes here
endfunction
```

---

```octave
np = n - 1;
while (np >= 1)
  if (is_even(np)) -- is_even is defined below
    -- zero in the binary expansion
    np = np / 2;
  else
    -- one in the binary expansion
    np = (np - 1) / 2;
  endif
  b *= p;
endwhile
p *= p;
endfunction
```

```octave
function e = is_even(n)
  ## Return true (1), if n is even, false (0) otherwise.
  e = (rem(n, 2) == 0)
endfunction
```
to C++. To this end, Octave’s core interface supplies the macro (in OCT/src/defun-int.h)

```cpp
octave_value_list DEFUN_DLD(function_name,
    const octave_value_list& input_argument_list,
    [ int number_of_output_arguments ],
    const char* documentation_string)
```

We have decorated the macro arguments with their types. Note that the first argument is the name of the function to be defined.

Of course the macro has to be defined somewhere. The easiest way to pull in all necessary definitions is to include OCT/src/oct.h. Now, our skeletal source file of the dynamic extension has the following shape:

```cpp
#include <oct.h>

DEFUN_DLD(func, args, nargout,
    "func frobs the snafu, returning the gromniz coefficients.")
{
    -- actual function code goes here

    return possibly_empty_list_of_values;
}
```

Often functions do not depend on the actual number of output parameters. Then, the third argument to DEFUN_DLD can be omitted.

**Naming convention:** DEFUN_DLD gives the user the freedom to choose any name for `input_argument_list` and `number_of_output_arguments`, but conventionally `args` and `nargout` are used (thus reminding of the parameter names in `main`, which are `argc` and `argv`).

### 1.1.3.2. Essential types and methods

Before we start to write a low-level implementation of `matpow`, we look at the most essential types and methods used to handle data that flows through the Octave-interpreter interface.

As has been said above, the arguments passed to dynamically loaded functions are bundled in an `octave_value_list`. Results returned from a function are also passed in an `octave_value_list`. The default constructor, `octave_value_list`, creates an empty list which, when used as return value, yields an Octave function returning “void”. To access the elements of a list the following methods form class `octave_value_list` (defined in OCT/src/oct-obj.h) are useful:

```cpp
class octave_value_list {
    public octave_value_list();
};
```
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public octave_value& operator()(int index);
public const octave_value operator()(int index);
public const int length();

}  

length returns the number of elements in the list. The overloaded parenthesis operator selects a single element from the list. The index base for index is 0 and not 1 as Fortran adepts might infer. The value returned by operator() is an octave_value, i.e., any type known to Octave, e.g. integers, real matrices, complex matrices, and so on.

Knowing how to access the arguments of unspecified type, the next thing we would like to do is get their values. Octave follows a uniform naming scheme: all functions that return an object of a certain type ends in _type. Some of the more important of these methods (defined in OCT/src/ov-base.h) are:

```cpp
class octave_base_value {
  public const int int_value();
  public const double double_value();
  public const Complex complex_value();
  public const Matrix matrix_value();
  public const ComplexMatrix complex_matrix_value();
}
```

1.1.3.3. Low-level implementation

Now, we are ready to implement matpow as a dynamically loaded extension to Octave.

**Example 1-3. C++ implementation of matpow**

```cpp
#include <octave/oct.h>

static bool is_even(int n);

DEFUN_DLD(matpow, args, ,
  "Return b = a^n for square matrix a, and non-negative, integral n."
) {
  const int n = args(1).int_value();  

  if (n == 0)
    return octave_value(
      DiagMatrix(args(0).rows() , args(0).columns() , 1.0)  
    );
  if (n == 1)
    return args(0);
  Matrix p(args(0).matrix_value());  
  Matrix b(p);
  int np = n - 1;
  while (np >= 1)
```


```cpp
{  
    if (is_even(np))  
    {  
        np = np / 2;  
    } 
    else  
    {  
        np = (np - 1) / 2;  
        b = b * p;  
    }  
    p = p * p;  
}
return octave_value(b);
}

bool is_even(int n)
{
    return n % 2 == 0;
}
```

1. Get the exponent \( n \), which is the second argument to `matpow` through `args(1)` and retrieve its integral value with `int_value`.
2. The matrix that we want to raise to the \( n \)-th power is the first argument, therefore it is accessed through `args(0)`. The method `rows` returns the number of rows in the matrix.
3. The method `columns` returns the number of columns in the matrix. (The actual value is assumed to be equal to the number of rows. At this stage, we are tacitly assuming that all parameters passed to `matpow` are valid, which means especially that the matrix is square.)
4. We call a constructor for diagonal matrices, `DiagMatrix` (defined in `OCT/liboctave/dDiagMatrix.h`), that accepts the size of the matrix and the value to put on the diagonal, which is 1 in our case.
5. Initialise the matrix \( p \) that will store the powers of the base. The `Matrix` constructor cannot take an `octave_value` and we have to supply the matrix itself by invoking `matrix_value`.
6. Multiplication has been conveniently overloaded to work on matrices. Wanna give John a treat for this one?

**Tip:** The Octave library overloads all elementary operations of scalars, (row-/column-) vectors and matrices. If in doubt as to whether a particular operation has been overloaded, simply try it. It takes less time than browsing (read: grep through) all the sources – the desired elementary operation is implemented in most cases.

7. We can return the result matrix \( b \) directly, as an appropriate constructor is invoked to convert it to an `octave_value_list`. 

---

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We learn from the example that the C++ closely resembles the Octave function. This is due to the clever class structure of the Octave library.

1.1.3.4. Compiling

Now that we are done with the coding, we are ready to compile and link. The Octave distribution contains the script `mkoctfile`, which does exactly this for us. In the simplest case it is called with the C++-source as its only argument.

```
$ ls
Makefile matpow0.m matpow1.m matpow.cc test_matpow.m
$ mkoctfile matpow.cc
```

Good, but not good enough! Presumably, we shall compile several times, so we would like to run our test suite and finally remove all files that can be re-generated from source. Enter: `Makefile`.

Example 1-4. Simple Makefile for oct-files

```
# Makefile for Octave extension matpow

.phony: all
all: matpow.oct

.phony: clean
clean:
  rm -f matpow.oct *.o

.phony: distclean
distclean: clean
  rm -f *~ octave-core core

.phony: test
test: matpow.oct
  octave --silent test_matpow.m

%.oct: %.cc
  mkoctfile $<
```

1.1.3.5. Running

If the `oct-file` is in the LOADPATH, it will be loaded automatically – either when requesting `help` on the function or when invoking it directly.

```
$ ls
Makefile matpow0.m matpow1.m matpow.cc matpow.o matpow.oct test_matpow.m
$ octave -q
```
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octave:1> help matpow
matpow is the dynamically-linked function from the file /home/cspiel/hsc/octave/src/matpow/matpow.oct
Return b = a^n for square matrix a, and non-negative, integral n.

octave:2> matpow([2, 0; 0, -1], 4)
   ans =
      16   0
       0   1
octave:3> Ctrl-D

1.1.4. Spicing up matpow

The keen reader will have noticed that matpow is highly vulnerable to unexpected input. We take care of this deficiency in Section 1.1.4.1. Also, the documentation is not ready for prime time, something we attend to in Section 1.1.4.2.

1.1.4.1. Input parameter checking

Why do we need parameter checking at all? A rule of thumb is to perform a complete parameter checking on

- every function that is exposed to the user (e.g. at Octave’s interpreter level), i.e. for every function created with DEFUN_DLD, or
- any function that might be used in a different context than the writer intended Functions that are used only internally do not require full parameter checking.

One problem which arises frequently with parameter checking of (interfacing) functions is that the checks easily take up more space than the routine itself, thereby distracting the reader from the function’s original purpose. Often, including all the checks into the main function bloats it beyond the desired maintainability. Therefore, we have to take precautions against these problems by consistently factoring out all parameter checks.

The rule of thumb here is to group logically related tests together in separate functions. The testing functions get the original functions’ arguments by constant reference and return a boolean value. Constant referencing avoids any constructor calls and – in addition to that – protects the arguments against modification. In our example a single test function is enough:

static bool any_bad_argument(const octave_value_list& args);
any_bad_argument prints a detailed message, raises an Octave error, and returns true if the arguments fail any test; otherwise it returns false and we can continue processing. The only thing we have to change in matpow is to add a call to any_bad_argument and on failure to return an Octave-void value, i.e. an empty octave_value_list. The first few lines of matpow then take the following form:

```
DEFUN_DLD(matpow, args, ,
   "Return b = a^n for square matrix a, and non-negative, integral n."
)
{
    if (any_bad_argument(args))
        return octave_value_list();

    const int n = args(1).int_value();

    -- rest of matpow is unchanged
}
```

As we are convinced that we have to check the input arguments, the question is how to do the checks.

**Ordering of Tests:** The correct ordering of tests is essential!

1. Actual number of arguments
2. Type of argument
3. Size of argument (where applicable)
4. Range of argument (where applicable and necessary)
5. Inter-argument relations (if necessary)

Item 1 always goes first. Items 2-4 usually repeat for each of the arguments. The final tests check the relations between the arguments, i.e., belong to Item 5.

Octave supplies the user with all necessary type- and size-testing functions. The type-tests (defined in OCT/src/ov-base.h) share the common prefix is_. Here are the most commonly used:

```
class octave_base_value, public class foo_value {
    public const bool is_real_scalar();
    public const bool is_complex_scalar();
    public const bool is_real_matrix();
    public const bool is_complex_matrix();
}
```

To examine the sizes of different Octave objects, the following methods prove useful:

```
class octave_list, public class octave_base_value {
    public const int length();
}

class octave_base_matrix, public class octave_base_value {
    public const int rows();
    public const int columns();
    public const int length();
}
```

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Remember that the methods available depend on the underlying type. For example, a ColumnVector only has a length (OCT/src/ov-list.h), whereas a Matrix has a number of rows and columns (OCT/src/ov-base-mat.h).

We have all the knowledge we need to write the argument testing function to augment matpow.

```c
static bool any_bad_argument(const octave_value_list& args) {
    if (!args(0).is_real_matrix()) {
        error("matpow: expecting base A (arg 1) to be a real matrix");
        return true;
    }
    if (args(0).rows() != args(0).columns()) {
        error("matpow: expecting base A (arg 1) to be a square matrix");
        return true;
    }
    if (!args(1).is_real_scalar()) {
        error("matpow: exponent N (arg 2) must be a real scalar.");
        return true;
    }
    if (args(1).scalar_value() < 0.0) {
        error("matpow: exponent N (arg 2) must be non-negative.");
        return true;
    }
    if (floor(args(1).scalar_value()) != args(1).scalar_value()) {
        error("matpow: exponent N (arg 2) must be an integer.");
        return true;
    }
    return false;
}
```

Out final duty is to update the test-frame and run it. For brevity, we only list the new tests in `testmp.m`:

```plaintext
### The following tests should trigger the error exits.
###
## number of arguments
```
unit_test_err("error exit, too few arguments",
            "matpow:", "matpow([1,1; 1,1])");

unit_test_err("error exit, too few arguments",
            "matpow:", "matpow()" );

unit_test_err("error exit, too many arguments",
            "matpow:", "matpow([1,1; 1 1], 2, 1)" );

## argument type and size

unit_test_err("error exit, A not a matrix",
            "matpow:", "matpow(1, 1)" );

unit_test_err("error exit, A not a square matrix",
            "matpow:", "matpow([1 2 3; 4 5 6], 1)" );

unit_test_err("error exit, N not a real scalar (here: complex)",
            "matpow:", "matpow(a, 1+i)" );

unit_test_err("error exit, N not a real scalar (here: non-scalar)",
            "matpow:", "matpow(a, ones(2,2))" );

unit_test_err("error exit, N negative",
            "matpow:", "matpow(a, -1)" );

unit_test_err("error exit, N non-integral",
            "matpow:", "matpow(2.5)" );

$ octave -q test_matpow.m
............
# of testcases attempted 16
# of expected passes 16
# of expected failures 0
# of unexpected passes 0
# of unexpected failures 0
# of unresolved testcases 0

Unit testing completed successfully!

1.1.4.2. Texinfo documentation strings

Our much improved \texttt{matpow} still carries around the poor documentation string:

"Return $b = a^n$ for square matrix $a$, and non-negative, integral $n$."
Let us improve on this one! Octave supports documentation strings – docstrings for short – in Texinfo format. The effect on the online documentation will be small, but the appearance of printed documentation will be greatly improved.

The fundamental building block of Texinfo documentation strings is the Texinfo-macro \texttt{@deftypefn}, which takes two arguments: the class the function is in, and the function’s signature. For functions defined with \texttt{DEFUN_DLD}, the class is \texttt{Loadable Function}. A skeletal Texinfo docstring therefore looks like this:

\textbf{Example 1-5. Skeletal Texinfo Docstring}

\begin{verbatim}
 -*- texinfo -*-
@deftypefn{Loadable Function} {\it return_values =} function_name(\it arguments)
\end{verbatim}

\begin{itemize}
\item[\textcircled{1}] Tell the parser that the doc-string is in Texinfo format.
\item[\textcircled{2}] \texttt{@deftypefn(class) ... @end deftypefn} encloses the whole doc-string, like a LaTeX environment or a DocBook element does.
\item[\textcircled{3}] \texttt{@cindex index entry} generates an index entry. It can be used multiple times.
\end{itemize}

Texinfo has several macros which control the markup. In the group of format changing commands, we note \texttt{@var{variable_name}}, and \texttt{@code{code_piece}}. The Texinfo format has been designed to generate output for online viewing with text-terminals as well as generating high-quality printed output. To these ends, Texinfo has commands which control the diversion of parts of the document into a particular output processor. Two formats are of importance: info and TeX. The first is selected with

\begin{verbatim}
@ifinfo
\end{verbatim}

the latter with

\begin{verbatim}
@iftex
@tex
\end{verbatim}

If no specific output processor is chosen, by default, the test goes into both (or, more precisely: every) output processors. Usually, neither \texttt{@ifinfo}, nor \texttt{@iftex} appear alone, but always in pairs, as the same information must be conveyed in every output format.
Example 1-6. Documentation string in Texinfo format

-*- texinfo -*-
@deftypefn{Loadable Function} {@var{b} =} matpow(@var{a}, @var{n})

@code{matpow}@code{()} duplicates part of the functionality of the built-in
exponentiation operator

Example:
@example
matpow([1, 2; 3, 4], 4)
@end example
returns
@example
ans =
  199  290
  435  634
@end example

The algorithm takes
@iftex
@tex
$\lfloor \log_{2}(n) \rfloor$
@end tex
@end iftex
@ifinfo
floor(log2(n))
@end ifinfo
matrix multiplications to compute the result.
@end deftypefn

1. @iftex ... @end iftex selects text for conditional inclusion. Only if the text is processed with an TeX the included section will be processed.

2. @tex ... @end tex wraps parts of the text that will be fed through TeX.

3. @ifdoc ... @end ifdoc selects text for conditional inclusion. Only if the text is processed with an info-tool the included section will be processed.

4. @code{code sequence} marks up a a code sequence.

5. @example ... @end example wraps examples.

For further information about Texinfo consult the Texinfo documentation. For TeX-beginners we recommend “The Not So Short Introduction to LaTeX” by Tobias Oetiker et. al.

One thing we held back is the true appearance of a Texinfo docstring – mainly because it looks so ugly. The C++-language imposes the constraint that the docstring must be a string-constant. Moreover, because DEFUN_DLD is a macro, every line-end has to be escaped with a backslash. The backslash does not insert any whitespace and TeX separates paragraphs with empty lines, so that we have to put in new-lines as line-separators. Thus, the Texinfo docstring in source form has each line end decorated with "\n".

DEFUN_DLD(matpow, args, ,
  "-*- texinfo -*-
  @deftypefn{Loadable Function} {@var{b}} = matpow(@var{a}, @var{n})
  
  @cindex matrix power
  
  Return matrix @var{a} raised to the @var{n}-th power. Matrix @var{a} is a square matrix, and @var{n} a non-negative integer. @var{n} = 0 is explicitly allowed, returning a unit-matrix of the same size as @var{a}.
  ...
")

At least the formatted versions look much better. The info-version, which will be used in Octave’s online help has approximately the following appearance:

b = matpow(a, n) Loadable Function
Return matrix a raised to the n-th power. Matrix a is a square matrix, and n a non-negative integer. n = 0 is explicitly allowed, returning a unit-matrix of the same size as a.

Note: matpow duplicates part of the functionality of the built-in exponentiation operator "^".

Example:
matpow([1, 2; 3, 4], 4)

returns
The algorithm takes \(\text{floor}(\log_2(n))\) matrix multiplications to compute the result.

whereas the TeX-version will look like this:

\[
b = \text{matpow}(a, n) \quad \text{[Loadable Function]}
\]

Return matrix \(a\) raised to the \(n\)-th power. Matrix \(a\) is a square matrix, and \(n\) a non-negative integer.

Return matrix \(a\) raised to the \(n\)-th power. Matrix \(a\) is a square matrix and \(n\) a non-negative integer. \(n = 0\) is explicitly allowed, returning a unit matrix of the same size as \(a\).

Note: \text{matpow} duplicates part of the functionality of the built-in exponentiating operator “\(^{}\)”.

Example:

\[
\text{matpow}([1, 2; 3, 4], 4)
\]

returns

\[
\text{ans} = \\
199 290 \\
435 634
\]

The algorithm takes \(\lfloor \log_2(n) \rfloor\) matrix multiplications to compute the result.

Docstring of \text{matpow} after rendering with TeX. Note the differences between the info-version and the TeX-version, that have been introduced with \texttt{@ifinfo} and \texttt{@iftex}.

1.2. Advanced Extension Programming

...

1.2.1. Defining Constants And Variables

The definition of constants and variables in a dynamically linked GNU/Octave extension resembles the header of a dynamically linked function (see, for example, Section 1.1.3). However, the appropriate macro \texttt{DEFCONST} is not available when creating a dynamically loadable extension for it is defined in \texttt{defun.h} and not in \texttt{defun-dld.h}. The latter is necessary to set up an dynamically loadable extension.
The easiest, moderately clean way is to duplicate DEFCONST’s definition from defun.h into the respective extension.

    // same definition as found in defun.h

#ifndef DEFCONST
#define DEFCONST(name, defn, doc) DEFCONST_INTERNAL(name, defn, doc)
#endif

DEFCONST introduces a constant named constant_name at the interpreter level, giving it the value of defining_expression and endowing it with the documentation documentation_string. The newly created constant will be protected against deletion, but not against change.

    void
DEFCONST(constant_name,
         defining_expression,
         const std::string& documentation_string)

The name of the constant constant_name must be a valid C++ identifier, because it is not quoted. Octave automatically casts the variable’s definition, defining_expression, to type octave_value.

A constant can be assigned to and then takes on the new value! Assigning to a constant does not even produce a warning. clearing a protected constant does not give raise to a warning either. Clearing a protected constants re-installs its original value.

Example 1-7. Constant Definition

    #include <oct.h>

    // 'DEFCONST' from "defun.h"
#ifndef DEFCONST
#define DEFCONST(name, defn, doc) \ 
    DEFCONST_INTERNAL(name, defn, doc)
#endif

static const double h = 6.626176e-34; // Planck’s constant in J*s

DEFUN_DLD(defconst, args, ,
    "Install some fundamental physical constants.")
{
    if (args.length() == 0)
    {
        DEFCONST(c, 2.99792458e8,
            "Speed of light in m/s.");
        DEFCONST(hbar, h / (2.0 * M_PI),
            "Reduced Planck’s constant hbar, that is, h/(2*pi) in J*s.");
        DEFCONST(G, 6.672e-11,
            "Gravitation constant in N*m^2/kg^2.");
        DEFCONST(e, 1.6021892e-19,
            "(Absolute value of the) Charge of an electron in C.");
    }
Tip: Long documentation strings in a long series of definitions tend to obscure the code. Assigning the documentation string to a macro allows for a separation of the help text and the definition.

#define DOCSTRING_HBAR \
"Reduced Planck’s constant hbar, this is, h/(2*pi) in J*s."
...
DEFCONST(hbar, h / (2.0 * M_PI), DOCSTRING_HBAR);

This is also useful for describing the function’s documentation string.

Like DEFCONST is defined in defun.h and not in defun-dld.h. So, the programmer must introduce the macro himself.

// same definition as found in defun.h

#ifndef DEFVAR
#define DEFVAR(name, defn, chgfcn, doc) \n    DEFVAR_INTERNAL(#name, SBV_ ## name, defn, false, chgfcn, doc)
#endif

void DEFVAR(variable_name, 
    defining_expression, 
    symbol_record::change_function changing_function, 
    const std::string& documentation_string)

The parameters variable_name, defining_expression, and documentation_string are analogous to those of DEFCONST. Only changing_function calls for further explanation.

changing_function is a pointer to a function that gets called whenever variable variable_name is given a new value. changing_function can be NULL if there is no function to call. change_function is defined in symtab.h

// symtab.h
typedef int (*change_function) (void);
A *changing_function* never takes on any parameters! Therefore, it must have a built-in knowledge of which interpreter variable to take care of. Usually, *changing_functions* correspond one-to-one with *variable_names*. Note the *changing_function* is called to initialize *variable_name* with the value of *defining_expression*. This means that *changing_function* is called at least once even if *variable_name* never gets changed within the interpreter. The return value 0 from *changing_function* signals success to the caller, any other value stands for failure.

**DEFVAR** installs and initializes a variable in the interpreter’s workspace. To access a variable or constant, *variables.h* declares three functions:

```c
#include <variables.h>

std::string builtin_string_variable ( const std::string& symbol_name );
int builtin_real_scalar_variable ( const std::string& symbol_name , double& value );
octave_value builtin_any_variable ( const std::string& symbol_name );
```

**Example 1-8. Variable Definition**

```c
#include <oct.h>
#include <variables.h> // for 'builtin_*_variable'

// 'DEFVAR' from "defun.h"
 ifndef DEFVAR
   #define DEFVAR(name, defn, chg_fcn, doc) 
       DEFVAR_INTERNAL(#name, SBV_ ## name, defn, false, chg_fcn, doc)
 endif

static double counter_var;
static unsigned count = 0;
static int counter_set();

//
// documentation strings
//

#define DOCSTRING_DEFVAR "Define two variables in the workspace: simple and counter.\n\nSee the respective documentations, that is,\n'help simple' and 'help counter'."

#define DOCSTRING_SIMPLE "Variable 'simple' is initialized to 0.5.\n\nIt is not linked to any low-level variable."

#define DOCSTRING_COUNTER "Variable 'counter' is initialized to 1.0.\n\nIt is linked to the C++ variable 'counter_var' in file 'defvar.cc'.\n\nWhenever 'counter' is assigned to the number of assignments
\n"
is printed."

//
// body
//

DEFUN_DLD(defvar, args, , DOCSTRING_DEFVAR)
{
  if (args.length() == 0)
  {
    DEFVAR(simple, 0.5, 0, DOCSTRING_SIMPLE);
    DEFVAR(counter, 1.0, counter_set, DOCSTRING_COUNTER);
  }
  else
  {
    error("defvar: expecting no arguments.");
  }

  return octave_value_list();
}

static int
counter_set()
{
  if (builtin_real_scalar_variable("counter", counter_var) == 0)
  {
    error("counter_set: internal error, non-existent variable");
    return 1;
  }

  count++;
  cout << "==> 'counter' has been assigned to " << count << " times;\n"
       << "==> its new value is " << counter_var << ".;\n"

  return 0;
}

1.2.2. Documenting Constants And Variables

Having studied Section 1.1.4.2, only one new Texinfo function is waiting: defvr.

-*- texinfo -*-
@defvr {Built-in Variable} my_own_variable
...
@end defvr
1.3. Abridged Quick-Reference

Question to Radio Erivan: “Is Octave lacking a Quick Reference?” Answer: “No, Octave ships with a very nice 3 page Quick Reference card, but it only describes the interpreter, not the library-interface.”

Coda has to fill in the gap. The library quick reference is called “abridged”, which is a fancy word for “incomplete”. According to the established 80-20 rule, the reader will find 80% of the functions she needs for usual programming jobs. The missing 20% will take 80% of the total coding time to hunt down.

All methods listed in this section have public access specification. Therefore, we have dropped the public modifiers in the class’ synopsis.

To generate an up-to-date class reference using doxygen, issue the command

```bash
doxxygen -g octave-dox
```

Edit `octave-dox`, set `EXTRACT_ALL` and `RECURSIVE` to YES and `INPUT` to the location of the Octave include files, e.g. `/usr/include/octave-2.1.50`. Now execute

```bash
doxxygen octave-dox
```

to generate the documentation in `./html`.

1.3.1. Types

We follow the old tradition from the days of Pascal and introduce first the types the Octave library works on.

Table 1-1. Types

<table>
<thead>
<tr>
<th>Type</th>
<th>Files</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>octave_value_list</td>
<td>oct-obj.h</td>
<td>Heterogenous container that is used in passing arguments to and from a dynamically loadable extension. I.e. the parameters and return values of a loadable function are mapped onto octave_value_lists. See Section 1.3.2.</td>
</tr>
<tr>
<td>octave_value</td>
<td>ov.h</td>
<td>Single element of an octave_value_list, which can hold any of Octave’s types.</td>
</tr>
</tbody>
</table>
## Type | Files | Description
--- | --- | ---
octave_matrix | ov-re-mat.h | Any of Octave’s real-valued matrix (Matrix, DiagMatrix) or vector types (RowVector, ColumnVector).
octave_complex_matrix | ov-cx-mat.h | Any of Octave’s complex-valued matrix (ComplexMatrix, ComplexDiagMatrix) or vector types (ComplexRowVector, ComplexColumnVector).
octave_bool_matrix | ov-bool-mat.h | ?
octave_char_matrix | ov-char-mat.h | ?
octave_scalar | ov-scalar.h | Real (double) valued, complex (Complex) valued, or boolean (bool) scalar.
RowVector | oct-obj.h, ov-re-mat.h, ov.h | Real (double) valued row vector; works like a matrix with a single row.
ComplexRowVector | oct-obj.h, ov-cx-mat.h, ov.h | Complex (double) valued row vector; works like a matrix with a single row.
ColumnVector | oct-obj.h, ov-re-mat.h, ov.h | Real (double) valued column vector; works like a matrix with a single column.
ComplexColumnVector | oct-obj.h, ov-cx-mat.h, ov.h | Complex (Complex) valued column vector; works like a matrix with a single column.
Matrix | ov-re-mat.h, | Real (double) valued matrix.
ComplexMatrix | ov-cx-mat.h, | Complex (Complex) valued matrix.
boolMatrix | ? | Matrix of booleans (bool).
charMatrix | ? | Matrix of characters (char).
DiagMatrix | ov-re-mat.h, ov.h | Real (double) valued diagonal matrix.
ComplexDiagMatrix | ov-cx-mat.h, ov.h | Complex (double) valued diagonal matrix.
Cell array | ov-cell.h, Cell.h, | Cell array.

### 1.3.2. List Operations

```cpp
class octave_value_list {
```
Chapter 1. OCT Files

```cpp
class octave_value_list
{
    octave_value_list();
    octave_value_list(const T & t);
    octave_value& operator[](int index);
    const octave_value operator[](int index);
    const int length();
    const bool empty();
    octave_value_list& prepend(const octave_value& val);
    octave_value_list& append(const octave_value& val);
    octave_value_list& append(const octave_value_list& lst);
    octave_value_list& reverse();
    const octave_value_list& splice(int offset, int length, const octave_value_list& lst);
    const octave_value_list& index(idx_vector & i);
};
```

Most of the methods in `octave_value_list` are self explaining. The default constructor, `splice`, and `index` require some explanation.

**Default Constructor.** The default constructor makes an empty list. When an empty list is returned from a dynamically loaded extension, the function at the interpreter level behaves lieka procedure, i.e. returns “void” in other words returns nothing.

**Converting Constructors.** `octave_value_list` defines constructors for the following types `T`: double, Matrix, DiagMatrix, RowVector, ColumnVector, Complex, ComplexMatrix, ComplexDiagMatrix, ComplexRowVector, ComplexColumnVector, char*, std::string, string_vector, Range, and octave_value_list.

`splice`. Replaces `length` elements of the list, starting at `offset`, and then inserts `lst`. See also Octave documentation of `splice`.

`index`. Extract elements at the index values given by `idx_vector i`.

### 1.3.3. Access to Value

```cpp
class octave_base_value {
    const bool bool_value();
    const int int_value();
    const int nint_value();
    const double double_value();
    const Complex complex_value();
    const double scalar_value();
    const std::string string_value();
    const Range range_value();
    const Octave_map map_value();
    const octave_stream stream_value();
    octave_function* function_value(bool silent);
    const Cell cell_value();
    const boolMatrix bool_matrix_value();
    const Matrix matrix_value();
    const ComplexMatrix complex_matrix_value();
};
```
const charMatrix char_matrix_value();
const octave_value_list list_value();
}

1.3.4. Type Classification

class octave_base_value, public class foo_value {
  const bool is_scalar_type();
  const bool is_bool_type();
  const bool is_complex_type();
  const bool is_constant();
  const bool is_numeric_type();
  const bool is_range();
  const bool is_real_scalar();
  const bool is_real_type();
  const bool is_string();
  const bool is_matrix_type();
  const bool is_char_matrix();
  const bool is_complex_matrix();
  const bool is_complex_scalar();
  const bool is_real_matrix();
  const bool is_all_va_args();
  const bool is_builtin_function();
  const bool is_cell();
  const bool is_defined();
  const bool is_dld_function();
  const bool is_empty();
  const bool is_function();
  const bool is_list();
  const bool is_magic_colon();
  const bool is_map();
  const bool is_stream();
  const bool is_true();
  const bool is_zero_by_zero();
}

Notes

1. Octave already has a matrix power operator, the caret “^”, which is more powerful than our example ever will be. This should not bother us.

2. Octave-forge contains a good unit testing framework. The framework provided here is very simple and only intended as a teaching aid.
Chapter 2. Building Standalone Applications

The libraries Octave itself uses, can be utilized in standalone applications. These applications then have access, for example, to the vector and matrix classes as well as to all the Octave algorithms.

The following C++ program, Example 2-1, uses class Matrix from liboctave.a or liboctave.so.

Example 2-1. “Hello World!” program using Octave’s libraries.

```cpp
#include <iostream>
#include "oct.h"

int main(void)
{
    std::cout << "Hello Octave world!\n";

    const int size = 2;
    Matrix a_matrix = Matrix(size, size);
    for (int row = 0; row < size; ++row)
    {
        for (int column = 0; column < size; ++column)
        {
            a_matrix(row, column) = (row + 1)*10 + (column + 1);
        }
    }
    std::cout << a_matrix;
    return 0;
}
```

`mkoctfile` can once again be used to compile our application:

```
$ mkoctfile --link-stand-alone hello.cc -o hello
$ ./hello
Hello Octave world!
 11 12
 21 22
```

§
Appendix A. Complete examples

This appendix gathers all examples that are either too long for the main text or are referenced (but not defined in) the main text.

A.1. Unit-test

A.1.1. unit_init.m

function unit_init(verbosity, global_vars)
    ## Initialize the global structure unittest_results, which is needed
    ## in all functions of the *unittest module. Debugging information
    ## is printed if verbosity==1. global_vars is a cell array of the
    ## names of the global variables used in the tests.
    ##
    ## e.g. unit_init(1, {"g", "a", "x"})

    global unittest_results;

    unittest_results.verbose = 0;
    unittest_results.eval_globals = {};
    if (nargin > 0)
        if (!isscalar(verbosity) || verbosity < 0 || verbosity > 1)
            warning("unit_init: verbose must be 0 or 1");
        else
            unittest_results.verbose = verbosity;
        endif
        if (nargin == 2 && iscell(global_vars))
            for i = 1:length(global_vars)
                unittest_results.eval_globals{i} = strcat("global ", global_vars{i}, ";");
            endfor
        else
            error("global_vars must be a cell array");
        endif
    endif
    if (nargin > 2)
        usage("expecting 2 arguments only");
    end
endif

    unittest_results.total = 0; # number of testcases attempted
    unittest_results.pass = 0; # number of expected passed
    unittest_results.fail = 0; # number of unexpected failures
    unittest_results/upass = 0; # number of unexpected passes
    unittest_results.xfail = 0; # number of expected failures
    unittest_results.unresolved = 0; # number of unresolved testcases
A.1.2. unit_test.m

function result = unit_test(test_title, expect_pass, actual_result)
    ## Function unittest compares the ACTUAL_RESULT of running
    ## a test (either 0 for failure, or 1 for success) with the
    ## expected outcome of the test EXPECT_PASS (either 0 for expecting
    ## a failure, or 1 for expecting pass). TEST_TITLE is the name of
    ## the test. All test results will be accompanied by the test’s
    ## title.
    ##
    ## The result of unittest is one of the following: UNRESOLVED: The
    ## test did neither return 0 nor 1. PASS: expected pass, got pass.
    ## FAIL: expected pass, got fail. UPASS: expected fail, got pass.
    ## XFAIL: expected fail, got fail.
    ##
    ## A call to unittest typically looks like this:
    ##
    ## unittest("scalar integer addition", 1, eval("1 + 1 == 2;"));
    
    global unittest_results;
    
    ## Sanity check input parameters
    if ( nargin < 3 | nargin > 4 )
        error("Function run_rest expects 3 or 4 parameters.");
    endif

    if (!isstr(test_title))
        error("Expecting TEST_TITLE (arg 1) to be a string.");
    endif

    if (expect_pass != 0 & expect_pass != 1)
        error("Expecting EXPECT_PASS (arg 2) to be 0 or 1.");
    endif

    unittest_results.total++;

    ## Take actions depending on what test result we expect
    ## (expect_pass), and what we actually got (actual_result).
    if (actual_result != 0 & actual_result != 1)
        result = "UNRESOLVED";
        unittest_results.unresolved++;
        if (actual_result == 2)
            printf("SYNTAX ERROR: %s\n", test_title);
        endif
        return;
    endif

    if (expect_pass == 1 & actual_result == 1)

result = "PASS";
if (unittest_results.verbose != 0)
    printf("PASS: %s\n", test_title);
else
    printf('.');
endif
unittest_results.pass++;
elseif (expect_pass == 1 & actual_result == 0)
    result = "FAIL";
    printf("FAIL: %s\n\n", test_title);
    unittest_results.fail++;
elseif (expect_pass == 0 & actual_result == 0)
    result = "XFAIL";
    printf("XFAIL: %s\n", test_title);
    unittest_results.xfail++;
elseif (expect_pass == 0 & actual_result == 1)
    result = "UPASS";
    printf("UPASS: %s\n", test_title);
    unittest_results.upass++;
Appendix A. Complete examples

A.1.6. erreval.m

function rv = erreval(error_prefix, try_str, catch_str)
    ## erreval() extends the built-in function eval(). Return 0 if
    ## try_str does not raise the error of type error_prefix, return 1
    ## otherwise.
    global unittest_results;
    for k = 1:length(unittest_results.eval_globals)
        eval(unittest_results.eval_globals{k});
    end
    rv = 0;
    try
        eval(try_str);
    catch
        rv = errcheck(error_prefix);
    end
endfunction

A.1.7. unit_results.m

function unit_results()
    ## Print the results from previous unittest calls in pretty format.
    global unittest_results;

    printf("\n");
    printf("# of testcases attempted %d", unittest_results.total);
    printf("# of expected passes %d", unittest_results.pass);
    printf("# of expected failures %d", unittest_results.xfail);
    printf("# of unexpected passes %d", unittest_results.upass);
    printf("# of unexpected failures %d", unittest_results.fail);
    printf("# of unresolved testcases %d", unittest_results.unresolved);
    printf("\n");

    if (unittest_results.total == unittest_results.pass + unittest_results.xfail)
        printf("Unit testing completed successfully!\n");
    else
        printf("One or more tests failed!\n");
    endif
endfunction
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Version 1.1, March 2000

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